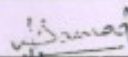


Batch 2019-20

ANSWER

PARTICULARS TO BE FILLED IN BY THE CANDIDATE		Question Booklet Number	
Name of the Candidate	ABDUL SAMAD	UEBT	01780
Roll Number	3351226		
Application Number	41077495		
Name of the Centre	University Polytechnic		
Centre Code	115	Paper Code	36
Date of the Test	26/05/2019	Question Paper Series	D
Signature of the Candidate			

Maximum Marks : 150

Test Duration : 03 hours

INSTRUCTIONS

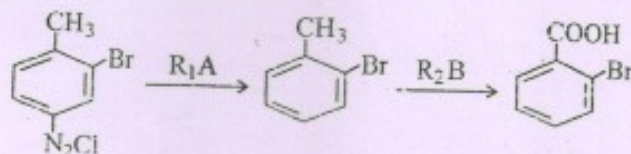
- Complete all entries on the cover page and put your signature in the space provided
- Use only Ball Point Pen (black / blue) for making entries in the Question booklet and the OMR Answer Sheet.

1. The Question Booklet consists of 48 pages and contains 150 questions. Count the number of pages and questions before attempting the questions. Discrepancy, if any, must immediately be brought to the notice of the Invigilator.
2. The Test duration as specified above shall be reckoned from the moment of distribution of the Question Booklets.
3. Blank space in the Question Booklet may be used for rough work.
4. Each question is followed by four alternative answers. Select only one answer, which you consider as the most appropriate. Shade the relevant circle against the corresponding question number on the OMR Answer Sheet. Selecting more than one answer for a question, even if one of the selected answers is correct, would result in its being treated as an incorrect answer.
5. Answers should ONLY be marked on the OMR Answer Sheet. No answer should be written / marked on the Question Booklet.
6. The candidate is required to separate the original OMR Answer Sheet and its carbonless copy at the perforation carefully after the Admission Test. He / She shall handover the original OMR Answer Sheet and the Admit Card to the Invigilator before leaving his / her seat and take with him / her the carbonless copy of the OMR Answer Sheet and the Question Booklet.
7. Failure to handover the original OMR Answer Sheet and the Admit Card will lead to cancellation of the candidature.



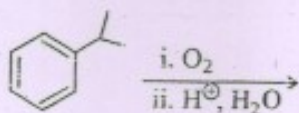
B-Tech 2019

1. Reagents R_1A and R_2B in the following reactions are



- (a) Sn, HCl and $\text{NaNO}_2, \text{HCl}$
 (b) $\text{H}_3\text{PO}_2, \text{H}_2\text{O}$ and $\text{KMnO}_4, \text{OH}^-$
 (c) HBF_4 and $\text{KMnO}_4, \text{OH}^-$
 (d) $\text{H}_3\text{PO}_2, \text{H}_2\text{O}$ and Sn, HCl
2. Select the correct group of compounds from the following that gave yellow precipitate on reaction with iodine and sodium hydroxide
- I. 1-Phenyl ethanol
 - II. Butan-2-ol
 - III. Pentan-3-ol
 - IV. Pentan-2-one
- (a) I, II, III
 (b) II, III, IV
 (c) I, II, IV
 (d) I, III, IV
3. Which one of the following compound is not prepared by Gabriel phthalimide synthesis?
- (a) PhNH_2
 (b) PhCH_2NH_2
 (c) $\text{C}_2\text{H}_5\text{NH}_2$
 (d) $\text{HC}\equiv\text{CCH}_2\text{NH}_2$

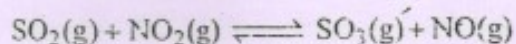
4. By-product of the following reaction is



- (a) Acetone
(b) Isopropyl alcohol
(c) Acetaldehyde
(d) Acetic acid
5. The correct order of increasing acidic nature of the following compound is
θ-Chlorophenol, θ-Cresol, θ-Nitrophenol, Picric acid
- I II III IV
- (a) I < II < III < IV
(b) II < I < III < IV
(c) III < II < I < IV
(d) I < III < II < IV
6. A linkage between two monosaccharide units through oxygen atom is known as
- (a) Peptide linkage
(b) Phosphodiester linkage
(c) Ester linkage
(d) Glycosidic linkage

7. In an adsorption experiment, a graph between $\log(n/m)$ versus $\log P$ was found to be linear with a slope of 45° and the intercept was 0.3010. The amount of the gas adsorbed per gram of charcoal under a pressure of 0.5 atm will be
- (a) 1.5
 - (b) 1.0
 - (c) 0.5
 - (d) 0.25
8. The melting point of benzene is 5.5°C . What is the sign of ΔH , ΔS and ΔG for melting point of benzene at 0°C
- (a) $\Delta H > 0$, $\Delta S > 0$, $\Delta G > 0$
 - (b) $\Delta H < 0$, $\Delta S > 0$, $\Delta G < 0$
 - (c) $\Delta H > 0$, $\Delta S > 0$, $\Delta G < 0$
 - (d) $\Delta H > 0$, $\Delta S < 0$, $\Delta G > 0$
9. When a direct current is passed through an aqueous concentrated solution of NaCl which statement is true?
- (a) pH of the solution decreases
 - (b) Chlorine gas will be liberated at the anode
 - (c) Metallic sodium will be deposited at the cathode
 - (d) Both (a) and (b) are true
10. B^- ions form a close packed structure. If the radius of B^- ion is 200 pm, then the cation (A^+) having radii 88 pm can fit into
- (a) tetrahedral hole
 - (b) octahedral hole
 - (c) both of them
 - (d) none of them

11. At a certain temp, equilibrium constant (K_c) is 16 for the reaction,



If one mole of each of the four gases are taken in one litre container, the equilibrium concentration of NO will be

- (a) 0.4 mole
 (b) 1.6 mole
 (c) 0.6 mole
 (d) 0.66 mole
12. The enthalpy of formation of water is,
 [Given that the bond energies of H-H, O=O and O-H bonds are 433 kJ/mol, 492 kJ/mol and 464 kJ/mol, respectively]

- (a) 430 kJ/mol
 (b) -249 kJ/mol
 (c) -461 kJ/mol
 (d) 215 kJ/mol

13. 2 moles PCl_5 were introduced in a 2 L flask and heated at 625 K to establish equilibrium when 60% of PCl_5 was dissociated into PCl_3 and Cl_2 . The equilibrium constant is

- (a) 0.90
 (b) 1.3
 (c) 0.128
 (d) 0.53

Handwritten calculations for Q13:

$$\frac{2.0}{100} \times 625 \times 2 \times 2000$$

$$\begin{array}{r} 125 \\ 1025 \\ -60 \\ \hline 25 \end{array}$$

$$\begin{array}{r} 25 \\ 150 \end{array}$$

14. The standard reduction potential for Zn^{2+}/Zn , Ni^{2+}/Ni and Fe^{2+}/Fe are -0.80 V, -0.25 V and -0.45 V, respectively. The reaction $\text{X} + \text{Y}^{2+} \rightarrow \text{X}^{2+} + \text{Y}$ will be spontaneous when

- (a) X = Ni, Y = Fe
 (b) X = Ni, Y = Zn
 (c) X = Zn, Y = Ni
 (d) X = Fe, Y = Zn

15. The Gibbs free energy for the decomposition of Al_2O_3 at 500°C is 482.5 kJ/mol . The potential difference needed for electrolytic reduction of Al_2O_3 at 500°C is at least
- (a) 2.5 V
 - (b) 5.0 V
 - (c) 1.25 V
 - (d) 4.5 V
16. The reaction is,
 $2\text{A} + \text{B} + \text{C} \rightarrow \text{A}_2\text{B} + \text{C}$, $k = 2 \times 10^{-6} \text{ mol}^{-2} \text{ L}^2 \text{ s}^{-1}$. The initial concentration of $[\text{A}] = 0.05 \text{ mol/L}$, $[\text{B}] = 0.1 \text{ mol/L}$ and $[\text{C}] = 0.5 \text{ mol/L}$. The rate after 0.04 mol/L of A has reacted, will be
- (a) 1.28×10^{-8}
 - (b) 1.28×10^{-10}
 - (c) 1.60×10^{-8}
 - (d) 1.60×10^{-10}
17. Which of the following is not a true statement?
- (a) Joule-Thomson effect is isoenthalpic process
 - (b) The positive value of μ_{JT} implies cooling effect
 - (c) The negative value of μ_{JT} implies cooling effect
 - (d) At inversion temperature, $\mu_{JT} = 0$
18. What will be solubility of $\text{KAl}(\text{SO}_4)_2$ in water if solubility product (K_{sp}) for $\text{KAl}(\text{SO}_4)_2$ is 1.6×10^{-11} (unit)
- (a) $6 \times 10^{-5} \text{ M}$
 - (b) $3 \times 10^{-4} \text{ M}$
 - (c) $2 \times 10^{-6} \text{ M}$
 - (d) $1.4 \times 10^{-3} \text{ M}$

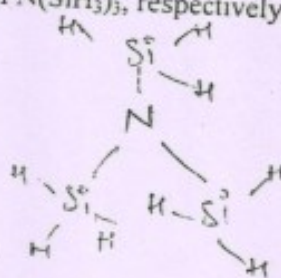
19. The following cell has a potential of 0.27 V at 25 °C
 $\text{Pt(s)} | \text{H}_2(\text{atm}) | \text{H}^+(\text{?M}) || \text{Ni}^{2+}(1\text{M}) | \text{Ni}$
 What is the pH of the solution in anodic compartment?
 (a) 2.6
 (b) 5.9
 (c) 8.9
 (d) 5.3
20. The solubility of a salt is 'S' and the solubility product is $4 S^3$. The ratio of cations to anions in the salt is
 (a) 1:1
 (b) 1:2
 (c) 1:4
 (d) 4:1
21. Which of the following is pH of solution formed by mixing 0.2 M NH_4Cl and 0.1 M NH_3 . The pOH of ammonia solution is 4.75?
 (a) 9.85
 (b) 7.05
 (c) 6.95
 (d) 8.95
22. The rate law for the reaction described by $\text{N}_2\text{O}_2(\text{g}) \rightarrow 2\text{NO}(\text{g})$ is first order in the concentration of $\text{N}_2\text{O}_2(\text{g})$. The expression for the time dependent behavior of the product concentration $[\text{NO}]$ is
 (a) $[\text{NO}] = 2[\text{N}_2\text{O}_2]_0(1 - e^{-kt})$
 (b) $[\text{NO}] = [\text{N}_2\text{O}_2]_0(1 - e^{-kt})$
 (c) $[\text{NO}] = 2[\text{N}_2\text{O}_2]_0 e^{-kt}$
 (d) $[\text{NO}] = [\text{N}_2\text{O}_2]_0 e^{-kt}$
 where $[\text{N}_2\text{O}_2]_0$ is the initial concentration of N_2O_2 i.e. constant

23. The conjugate acid of O^{2-} is
 (a) O_2
 (b) O_2^-
 (c) H_2O
 (d) OH^-
24. The oxidation states of Pt in $[Pt(NH_3)_4][PtCl_4]$ is
 (a) +1 and +1
 (b) +1 and +2
 (c) +2 and +2
 (d) +2 and +1
25. The most common oxidation state in lanthanide group is
 (a) +2
 (b) +3
 (c) +4
 (d) +6
26. Correct order of Lewis acid character of boron trihalides is
 (a) $BF_3 > BCl_3 > BBr_3$
 (b) $BF_3 > BBr_3 > BCl_3$
 (c) $BCl_3 > BF_3 > BBr_3$
 (d) $BBr_3 > BCl_3 > BF_3$
27. The hybridization and geometry in $N(SiH_3)_3$, respectively, are
 (a) sp^3 , tetrahedral
 (b) sp^3 , pyramidal
 (c) sp^2 , triangular planar
 (d) sp^3d , T-shaped

$$x + 4(-2) = 0$$

$$x = 24 =$$

$$x$$



28. The number of P–O–P bonds in trimetaphosphoric acid is/are
- (a) 0
 - (b) 2
 - (c) 3
 - (d) 6
29. Which of the following ions has zero CFSE in octahedral field?
- (a) Cr^{3+} (high spin)
 - (b) Co^{2+} (low spin)
 - (c) Fe^{3+} (low spin)
 - (d) Fe^{3+} (high spin)
30. The basicities of H_3PO_3 and $\text{H}_4\text{P}_2\text{O}_7$, respectively, are
- (a) 1 and 4
 - (b) 2 and 4
 - (c) 3 and 4
 - (d) 2 and 3
31. The complexes $[\text{Ni}(\text{CO})_4]$ and $[\text{Ni}(\text{CN})_4]^{2-}$ are, respectively
- (a) tetrahedral and square planar
 - (b) tetrahedral and tetrahedral
 - (c) square planar and square planar
 - (d) square planar and tetrahedral
32. According to VSEPR theory, the geometry of ammonia and water molecules will, respectively, be
- (a) pyramidal and bent
 - (b) tetrahedral and pyramidal
 - (c) bent and pyramidal
 - (d) pyramidal and tetrahedral

33. Crystal field splitting energy for octahedral (Δ_0) and tetrahedral (Δ_t) complexes is related as

(a) $\Delta_t \approx \frac{4}{9} \Delta_0$

(b) $\Delta_t \approx \frac{1}{2} \Delta_0$

(c) $\Delta_0 \approx 2\Delta_t$

(d) $\Delta_0 \approx \frac{4}{9} \Delta_t$

34. The number of S-S bonds in sulphur trioxide trimer (S_3O_9) is

(a) 3

(b) 2

(c) 1

(d) 0



35. Which of the following system has maximum number of unpaired electrons?

(a) d^6 (tetrahedral, high spin)

(b) d^3 (octahedral)

(c) d^4 (octahedral, low spin)

(d) d^7 (octahedral, high spin)

36. Basicity of dithionic acid is

(a) Two

(b) One

(c) Three

(d) Four

37. Catalyst used for the following reaction $2I^- + S_2O_8^{2-} \rightarrow I_2 + 2SO_4^{2-}$

- (a) Fe powder
- (b) Fe^{+2}
- (c) Fe^{3+}
- (d) Pt

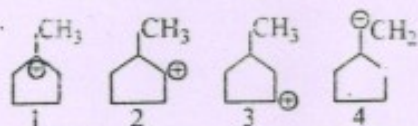
38. The test of NO_3^- ion through formation of brown ring is accompanied by reduction of NO_3^- ion into NO by an ion

- (a) H_3O^+
- (b) OH^-
- (c) Fe^{2+}
- (d) Fe^{3+}

39. The species analogous to paramagnetic behaviour like O_2

- (a) Monoclinic sulphur
- (b) Rhombic sulphur
- (c) Colloidal sulphur
- (d) Gaseous sulphur

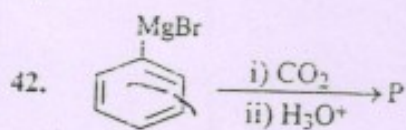
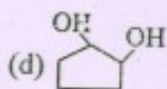
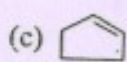
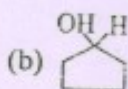
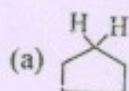
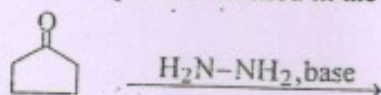
40. Consider the following carbocations



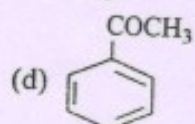
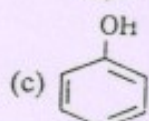
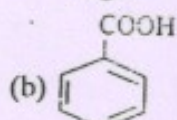
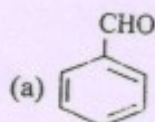
The decreasing order of stability of these carbocations will be

- (a) $1 > 2 > 3 > 4$
- (b) $1 > 3 > 2 > 4$
- (c) $1 > 3 > 4 > 2$
- (d) $1 > 2 > 4 > 3$



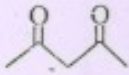
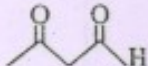
41. Select the product formed in the following reaction



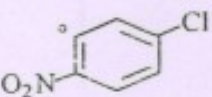
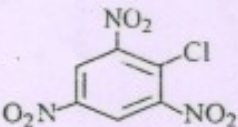
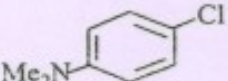
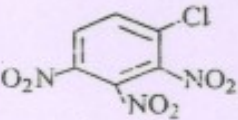
In the above reaction, product P is



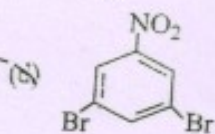
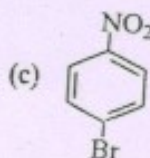
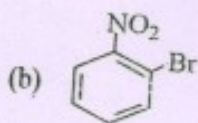
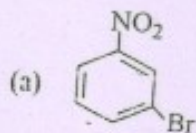
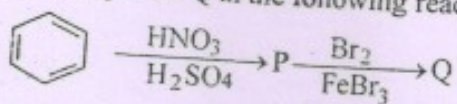
43. The maximum enol content is in

- (a) 
- (b) 
- (c) 
- (d) 

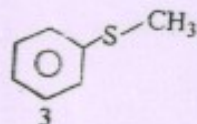
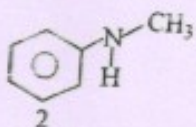
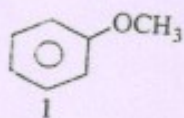
44. Which of the following derivatives of benzene would undergo hydrolysis most readily with aq. KOH?

- (a) 
- (b) 
- (c) 
- (d) 

45. The compound Q in the following reaction is

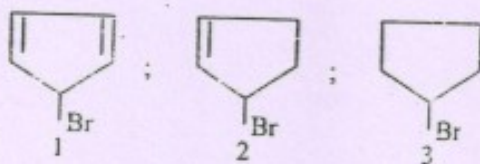


46. The decreasing order reactivity of the following compounds towards aromatic electrophilic substitution reaction will be



- (a) $1 > 2 > 3$
 (b) $3 > 2 > 1$
 (c) $1 > 3 > 2$
 (d) $2 > 3 > 1$

47. A dibromoalkane reacts with sodium metal to give an alicyclic hydrocarbon. The dibromoalkane is
- 1, 1-dibromopropane
 - 2, 2-dibromobutane
 - 1, 2-dibromoethane
 - 1, 4-dibromobutane
48. The correct decreasing order of acidic strength of (A) trichloroacetic acid (B) trifluoroacetic acid (C) acetic acid (D) formic acid is
- $A > B > C > D$
 - $A > C > B > D$
 - $B > A > D > C$
 - $B > A > C > D$
49. The gas evolved when methylamine reacts with nitrous acid is
- Nitrogen
 - Hydrogen
 - Acetylene
 - Ammonia
50. The decreasing order of rate of S_N1 reaction in the following compounds will be



- $3 > 2 > 1$
- $1 > 2 > 3$
- $1 > 3 > 2$
- $2 > 3 > 1$

51. A tractor has its rear wheel with radius 1.0 m and front wheel of radius 0.25 m. The rear wheel is rotating at 100 rev/min. Calculate the angular speed of the front wheel and the distance covered by the tractor in 10 minutes

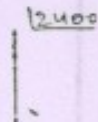
- (a) 400 rev/min, 6.28×10^3 m
- (b) 300 rev/min, 5.17×10^3 m
- (c) 200 rev/min, 3.14×10^3 m
- (d) 100 rev/min, 1.57×10^3 m



52. A stone is thrown from the top of a building with an initial downward velocity of 20 m/s. The top of the building is 60 m above the ground. Calculate the time taken (in seconds) by the stone to hit the ground

(Given $g = 10 \text{ m/s}^2$)

- (a) 2
- (b) 3
- (c) 4
- (d) 5



$$\begin{aligned}
 P.E &= mgh \Rightarrow \\
 P.E &= 20 \times 1 \times 60 \\
 P.E &= 1200 \\
 P.E &= K.E \\
 K.E &= \frac{1}{2} mv^2 \\
 1200 &= \frac{1}{2} v^2 \\
 2400 &= v^2
 \end{aligned}$$

53. If $\vec{A} = \vec{i} - \vec{j}$ and $\vec{B} = 3\vec{i} + 4\vec{j}$, the vector having same magnitude as \vec{B} but parallel to vector \vec{A} can be written as

- (a) $5(\vec{i} - \vec{j})$
- (b) $(5/\sqrt{2})(\vec{i} - \vec{j})$
- (c) $\sqrt{2}(4\vec{i} - 3\vec{j})$
- (d) $\sqrt{3}(\vec{i} + \vec{j})$

54. A father is racing with his son has half the kinetic energy of the son who has half the mass of the father. If the father speeds up by 1 m/s then he would have the same kinetic energy as the son. Calculate the original speed (in m/s) of the father

- (a) 2.4
(b) 3.2
(c) 4.6
(d) 5.8

$$\Rightarrow \frac{1}{2} = 1 + 2v \quad K \cdot E_F = \frac{1}{2} m v^2 = K E_S m(v+1)^2$$

$$\Rightarrow \frac{1}{4} + 1 = 2v \quad K \cdot E_S = \frac{1}{2} m v^2$$

$$\Rightarrow \frac{5}{4} = 2v \quad \frac{1}{2} m v^2 = m(v+1)^2$$

$$\Rightarrow \frac{5}{8} = v \quad \frac{1}{2} m v^2 = m(v^2 + 1 + 2v)$$

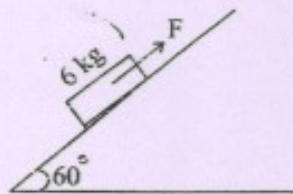
$$\Rightarrow \frac{5}{8} m v^2 = m v^2 + 1 + 2v$$

$$\frac{1}{4} = 1 + 2$$

$$\frac{1}{8} = \frac{1}{2} +$$

55. A 6.0 kg block is placed on a 60° ramp as shown in the figure. The coefficient of static friction is 0.6. A force \vec{F} is applied that puts the block on the verge of sliding down the ramp. The value of force F in Newtons is

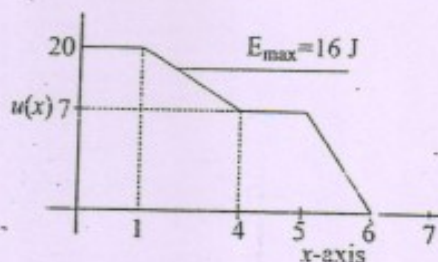
(Given: $\sqrt{3} = 1.73$ and $g = 9.8 \text{ m/s}^2$)



$$F = 6(\cos 60^\circ) \times 9.8$$

- (a) 23
(b) 33
(c) 45
(d) 57

56. A particle of mass 2 kg is moving towards the origin along x with total kinetic energy 16 J. It encounters a region where the potential energy $u(x)$ is shown in the figure. Calculate its velocity when its distance $x = 4.5$ m and the position of turning point



- (a) $(-9 \text{ m/s})\vec{i}$, 2.5 m
 (b) $(-7 \text{ m/s})\vec{i}$, 3.1 m
 (c) $(-3 \text{ m/s})\vec{i}$, 1.9 m
 (d) $(-1.5 \text{ m/s})\vec{i}$, 1.2 m
57. A 5.0 g bullet moving at 100 m/s strikes a wooden block. Assuming that the bullet undergoes a uniform deceleration and stops after penetrating a distance of 5 cm. The time taken by the bullet to stop and the impulse on the block are respectively
- (a) 4.5 ms and 3.2 N-S
 (b) 3.5 ms and 2.1 N-S
 (c) 2.7 ms and 1.5 N-S
 (d) 1.0 ms and 0.5 N-S

$$v = 2at$$

$$v = 2 \times 100$$

58. Calculate the height ' h ' above Earth's surface where the acceleration due to gravity would be 2.5 m/s^2
(Given $g = 10 \text{ m/s}^2$ and radius of the Earth = R_E)
- (a) $0.5 R_E$
(b) $1.0 R_E$
(c) $1.2 R_E$
(d) $1.5 R_E$
59. The dimensional formula for pressure gradient of a liquid flowing in a tube is
- (a) ML^2T^{-2}
(b) $ML^{-1}T^{-2}$
(c) MLT^{-2}
(d) $ML^{-2}T^{-2}$
60. A 31.4 kg girl wearing high heel shoes balances her weight on a single heel. The diameter of the heel is 1 cm . The pressure (in Pascal) exerted by the heel on the floor is
(Take $g = 10 \text{ m/s}^2$)
- (a) 2×10^6
(b) 4×10^6
(c) 6×10^6
(d) 8×10^6
61. X-rays of wavelength 0.15 nm on a silicon crystal. The first strong maximum is observed when the X-ray beam makes an angle of 30° with the planes. Calculate the distance between the planes of the silicon crystal
- (a) 0.15 nm
(b) 0.30 nm
(c) 0.45 nm
(d) 0.60 nm

$$0.15 \times \frac{0.52}{10} = \frac{0.078}{10} = \frac{0.0078}{1} = 0.0078$$

62. A transformer operates at $V_p = 9$ kV on the primary side and supplies electricity to a number of houses at $V_s = 120$ V (both quantities are rms values). If the total power consumption of the houses is 8 kW, estimate the current (in Amperes) in the primary and secondary of the transformer.
- 12 and 800
 - 9 and 667
 - 6 and 525
 - 3 and 450
63. A 5 mole bubble of Helium gas (monoatomic) is submerged to a certain depth in water which undergoes an increase of 10°C in its temperature. How much energy is added to the Helium bubble as heat during the increase in its temperature and its consequent expansion? (Take $R = 8.31$ J/mole-K)
- 625 J
 - 1040 J
 - 1250 J
 - 2325 J
64. The Earth's electric field 150 N/C (directed downward) acts on the electrons knocked out from the air molecules by the incoming cosmic rays. The work done (in Joules) in lifting an electron 500 meter upward from Earth's surface is (Electric charge on an electron $\cong 1.6 \times 10^{-19}$ Coulombs)
- 3.0×10^{-14}
 - 1.8×10^{-14}
 - 1.5×10^{-14}
 - 1.2×10^{-14}
65. An illuminated slide is held 50 cm from a screen. How far from the slide a lens of focal length 10 cm be placed (between the slide and screen) to form an image of the slide on screen?
- 25 cm
 - 21.3 cm
 - 13.5 cm
 - 8.2 cm

66. A block of density $\rho = 800 \text{ kg/m}^3$ floats face down in a liquid of density 1200 kg/m^3 . The block is 6 cm high. Calculate the depth 'h' of the block submerged in the liquid

- (a) 2.5 cm
- (b) 4.0 cm
- (c) 5.0 cm
- (d) 5.5 cm

67. Calculate the energy released during the alpha decay of ${}^{238}_{92}\text{U}$. Given the following data:

$${}^{238}_{92}\text{U} = 238.05079 \text{ u}$$

$${}^{234}_{90}\text{Th} = 234.04363 \text{ u}$$

$${}^4_2\text{He} = 4.00260 \text{ u}$$

$$1 \text{ u} = 931.5 \text{ MeV}$$

- (a) 4.25 MeV
- (b) 3.75 MeV
- (c) 3.50 MeV
- (d) 2.75 MeV

$${}^{238}_{92}\text{U} + \gamma \rightarrow {}^{234}_{90}\text{Th} + {}^4_2\text{He}$$

$$238.05079 + 0 \rightarrow 234.04363 + 4.00260$$

$$\begin{array}{r} 238.05079 \\ - 234.04363 \\ \hline 4.00716 \\ - 4.00260 \\ \hline 0.00456 \end{array}$$

$$\begin{array}{r} 4.00716 \\ - 4.00260 \\ \hline 0.00456 \end{array}$$

$$\begin{array}{r} 0.00456 \\ \times 931.5 \\ \hline 4.25 \end{array}$$

68. In an n-type semiconductor which of the following statement is true

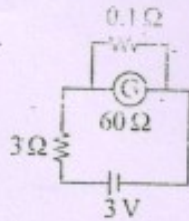
- (i) Electrons are majority carriers and trivalent atoms are the dopants
 - (ii) Electrons are minority carriers and pentavalent atoms are the dopants
 - (iii) Holes are minority carriers and pentavalent atoms are the dopants
 - (iv) Holes are majority carriers and trivalent atoms are the dopants
- (a) (i)
 - (b) (i) and (ii)
 - (c) (iii)
 - (d) (ii) and (iv)

69. A sinusoidal wave travels along a string. The time for a particular point of the string to move from maximum displacement to zero is 0.125 seconds. Calculate the time period and speed of the wave respectively if its wavelength is 1.4 m.
- (a) 0.5 s and 2.8 m/s
 - (b) 1.0 s and 1.4 m/s
 - (c) 1.5 s and 2.8 m/s
 - (d) 2.0 s and 1.4 m/s
70. A point source of light is 1.2 m below the surface of water. Estimate the diameter of the circle at the surface through which light emerges from the water (Given the refractive index of water to be 1.3)
- (a) 2.8 m
 - (b) 3.5 m
 - (c) 4.2 m
 - (d) 4.5 m
71. Two sinusoidal waves of equal amplitude Y_m and wavelength λ travel in opposite direction along a stretched string to produce standing waves. The third antinode is located at a distance from one end is
- (a) $3/2 \lambda$
 - (b) $5/4 \lambda$
 - (c) $7/2 \lambda$
 - (d) 3λ
72. In a photoelectric experiment with a certain monochromatic light a reverse 1.25 V potential is required to reduce the current to zero. Calculate the maximum speed of the photoelectrons (Given mass of the electron = 9×10^{-31} kg, charge of electron = 1.6×10^{-19} C)
- (a) 6.6×10^5 m/s
 - (b) 5.75×10^5 m/s
 - (c) 5.15×10^5 m/s
 - (d) 4.85×10^5 m/s

73. The energy of electron in quantum state n in Hydrogen atom is given by the relation $E_n = -\frac{hCR}{n^2}$. If the ground state energy is -13.6 eV then the energy of electron in the second excited state is
- (a) -6.8 eV
 (b) -4.5 eV
 (c) -3.4 eV
 (d) -1.5 eV
74. The kinetic energy of a given electron is five times more than a certain proton. How much the de-Broglie's wavelength of electron is bigger than the corresponding wavelength of the proton (Assume that both particles are non-relativistic and $m_p = 2000 m_e$)
- (a) 10
 (b) 20
 (c) 30
 (d) 40
75. A Carnot engine has an efficiency of only 15%. If it operates between constant temperature reservoirs differing in temperatures by 55°C the temperature of higher temperature reservoir is
- (a) 367°K
 (b) 382°K
 (c) 418°K
 (d) 421°K
76. Tritium's half-life is 12.5 years for beta decay. What fraction of pure Tritium would remain undecayed after 50 years?
- (a) $1/4$
 (b) $1/8$
 (c) $1/16$
 (d) $1/24$

77. The diffraction pattern of the 633 nm laser light through a single straight slit is observed on a screen 6 m away. The distance between the centres of the first minima outside the central bright fringe is 32 mm. The width of the slit is
- (a) 0.85 mm
 - (b) 0.75 mm
 - (c) 0.45 mm
 - (d) 0.24 mm
78. The wavelength of Helium-neon laser in air is 585 nm. As it enters the eye its wavelength changes to 450 nm. Calculate the velocity of the laser light inside the eyeball
- (a) 2.1×10^8 m/s
 - (b) 2.3×10^8 m/s
 - (c) 2.5×10^8 m/s
 - (d) 2.8×10^8 m/s
79. A circular coil of radius 10 cm, 500 turns of wire of total resistance 2Ω is placed with its plane perpendicular to the horizontal component of the Earth's magnetic field. It is rotated about its vertical diameter by 180° in 0.25 seconds. Estimate the induced e.m.f. in the coil (Given the horizontal component of Earth's field = 3×10^{-5} T)
- (a) 4×10^{-3} V
 - (b) 6×10^{-3} V
 - (c) 8×10^{-3} V
 - (d) 10×10^{-3} V
80. You are given a thin diverging lens of 20 cm focal length. Calculate the distance at which an object should be placed to obtain $1/3$ lateral magnification
- (a) 10 cm
 - (b) 30 cm
 - (c) 40 cm
 - (d) 50 cm

81. The value of current (in Amperes) through the $3\ \Omega$ resistance in the circuit as shown is



$$\frac{1}{R} = \frac{1}{0.1} + \frac{1}{60}$$

$$\frac{1}{R} = \frac{1}{6} \quad R = 6$$

- (a) 0.05 A
(b) 0.25 A
(c) 0.76 A
(d) 0.96 A
82. A 100 V power supply is used to charge a $2.5\ \mu\text{F}$ capacitor which is then connected to a 10 mH inductor. The frequency of the oscillating LC circuit is
- (a) 3.14 ms
(b) 2.50 ms
(c) 1.25 ms
(d) 1.00 ms
83. The resistance of the platinum wire of the platinum resistance thermometer at ice point is $5\ \Omega$ and at steam point is $5.25\ \Omega$. This thermometer is inserted in a hot liquid then its resistance is $5.75\ \Omega$. Calculate the temperature of the hot liquid (in $^{\circ}\text{C}$)
- (a) 300
(b) 250
(c) 200
(d) 150

84. A 3.6 A current flows through the headlights of a car. The total charge (Coulombs) flowed through the lights in 3 hours is nearly
- (a) 4×10^4
 - (b) 3.6×10^4
 - (c) 5.2×10^4
 - (d) 6.4×10^4

85. A 12 volts battery with 1Ω internal resistance is connected to a 5Ω external resistance. The rate of dissipation of electrical energy in the battery and the rate of conversion of internal chemical energy to electrical energy (in Watts) are
- (a) 10, 12
 - (b) 8, 16

79.

- Estimate the magnetic field at the center of a circular wire of radius r carrying a current i . The wire is placed in a uniform magnetic field B perpendicular to the plane of the wire.
- (a) $4 \times 10^{-3} \text{ T}$
 - (b) $6 \times 10^{-3} \text{ T}$
 - (c) $8 \times 10^{-3} \text{ T}$
 - (d) $10 \times 10^{-3} \text{ T}$

80. You are given a thin rod of length l and mass m suspended from a pivot at a distance x from one end. The rod is released from a horizontal position. The angular velocity of the rod at the instant it is vertical is ω . The value of x is
- (a) 10 cm
 - (b) 30 cm
 - (c) 40 cm
 - (d) 50 cm

are being accelerated in a cyclotron where the dees and a battery of V volts are used to accelerate the protons. The number of protons accelerated is

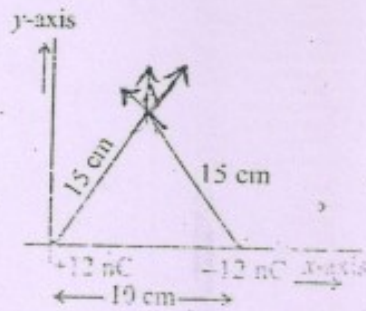
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net electric flux ($\text{C}^2/\text{N}\cdot\text{m}^2$)

$\times 10^{-12}$

UEBT/D

88. Two equal and opposite charges 12 nC are placed 10 cm apart on the x -axis as shown in the figure. Calculate the net electric field at 'A' equidistant (15 cm) from the charges as shown (in proper SI units)



$$\frac{1}{4\pi\epsilon_0} = \frac{q_1q_2}{r^2}$$

$$9 \times 10^9 \times \frac{12 \times 10^{-9}}{15 \times 15}$$

$$9 \times 10^9 \times 10^{-18} < 10^{-18}$$

$$\frac{9 \times 10^9 \times 10^{-18}}{15 \times 15}$$

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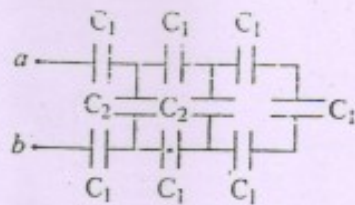
- (a) 1.5×10^3
 (b) 3.2×10^3
 (c) 6.4×10^3
 (d) 3.3×10^3

89. Two protons and an alpha particle respectively are held at the corners of an equilateral triangle with side length $8 \times 10^{-10} \text{ m}$. The particles are released and move apart. Their total energy when they are far apart is

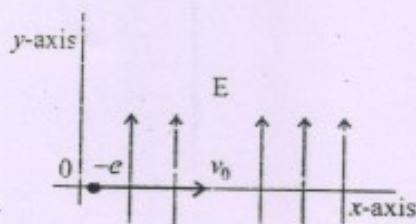
(Given : charge on a proton = $1.6 \times 10^{-19} \text{ C}$ and $\frac{1}{4\pi\epsilon_0} = 9 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2$)

- (a) $4.8 \times 10^{-18} \text{ J}$
 (b) $1.6 \times 10^{-18} \text{ J}$
 (c) $3.2 \times 10^{-18} \text{ J}$
 (d) $1.44 \times 10^{-18} \text{ J}$

90. In the figure shown, each capacitor C_1 is $6.9 \mu\text{F}$ and C_2 is $4.6 \mu\text{F}$. Calculate the equivalent capacitance between points 'a' and 'b'.



- (a) $48.3 \mu\text{F}$
 (b) $9.2 \mu\text{F}$
 (c) $11.5 \mu\text{F}$
 (d) $23 \mu\text{F}$
91. An electron (mass m and charge $-e$) is fired along x -axis with a velocity \vec{v}_0 in an area with uniform electric field \vec{E} along y -axis as shown in the figure. The trajectory of the electron is given by the relation



- (a) $y = -\frac{2eE}{mv_0} x^2$
 (b) $y = -\frac{1}{2} \frac{eE}{mv_0^2} x^2$
 (c) $y = -\frac{2eE^2}{mv_0^2} x$
 (d) $y = -\frac{1}{2} \frac{(eE)^2}{mv_0^2} x$

92. An Earth's satellite is moving with a linear velocity v . Its altitude h is given by the following relation (Given Mass of Earth = M_E , Radius of Earth = R_E)

(a) $h = \frac{GR_E}{M_E} - R_E$

(b) $h = \frac{GM_E}{v} - \frac{v}{R_E}$

(c) $h = \frac{GM_E}{v^2} - R_E$

(d) $h = \frac{GR_E}{v^2} - \frac{vM_E}{R_E}$

93. An ambulance producing siren with frequency 300 Hz is moving in the positive x -axis direction with velocity 45 m/s. Calculate the apparent frequency to a listener moving also in the positive x -axis direction with speed 15 m/s.

(a) 277 Hz

(b) 330 Hz

(c) 315 Hz

(d) 345 Hz

Handwritten calculations for Q93:
 $\frac{300 \times 45}{45 + 15} = 300 \times \frac{45}{60} = 300 \times \frac{3}{4} = 225$
 (Note: The handwritten work shows a result of 225 Hz, which is not among the options.)

94. The number of moles in 1 kg water is

(a) 18.0

(b) 25.7

(c) 32.5

(d) 55.6

12

95. A steam engine delivers 5.4×10^8 J of work per minute and absorbs 3.6×10^9 J of heat per minute from the boiler. Calculate the efficiency of the engine

- (a) 30%
- (b) 25%
- (c) 20%
- (d) 15%

96. Two monoatomic gases are kept at the same temperature. Their mass numbers are 36 and 25 respectively. Calculate the percentage difference in their rms speeds

- (a) 40%
- (b) 30%
- (c) 20%
- (d) 10%

97. A body is executing SHM according to the relation (in S.I. units)

$$x = 5\sqrt{2} \cos(2\pi t + \pi/4)$$

Its acceleration at $t = 1$ seconds is nearly

- (a) 200 m/s^2
- (b) 175 m/s^2
- (c) 150 m/s^2
- (d) 100 m/s^2

98. The gauge pressure produced by a machine to suck mud of density 1800 kg/m^3 up a tube by a height of 2.0 m from ground is
(Take $g = 9.8 \text{ m/s}^2$)
- (a) $2.0 \times 10^4 \text{ Pa}$
 - (b) $3.5 \times 10^4 \text{ Pa}$
 - (c) $6.2 \times 10^4 \text{ Pa}$
 - (d) $9.8 \times 10^4 \text{ Pa}$
99. An anchor of a ship, made of iron with density 7870 kg/m^3 appears 210 N lighter in water. Calculate the volume of anchor and its weight in air
(Take $g = 9.8 \text{ m/s}^2$)
- (a) $1.78 \times 10^{-2} \text{ m}^3$; 2.10 KN
 - (b) $2.14 \times 10^{-2} \text{ m}^3$; 1.65 KN
 - (c) $5.87 \times 10^{-2} \text{ m}^3$; 3.75 KN
 - (d) $7.87 \times 10^{-2} \text{ m}^3$; 5.67 KN
100. The coefficient of volume expansion of glycerin is $49 \times 10^{-5} \text{ K}^{-1}$. Calculate the fractional change in its density for a 30°C rise in its temperature
- (a) 4.9×10^{-2}
 - (b) 3.2×10^{-2}
 - (c) 1.5×10^{-2}
 - (d) 0.8×10^{-2}

101. Let α and β be the roots of the quadratic equation

$$x^2 \sin \theta - x(\sin \theta \cos \theta + 1) + \cos \theta = 0$$

$$\left(0 < \theta < \frac{\pi}{4}\right) \text{ and } \alpha < \beta.$$

Then $\sum_{n=0}^{\infty} \left(\alpha^n + \frac{(-1)^n}{\beta^n} \right)$ is equal to

(a) $\frac{1}{1 - \cos \theta} + \frac{1}{1 + \sin \theta}$

(b) $\frac{1}{1 + \cos \theta} + \frac{1}{1 - \sin \theta}$

(c) $\frac{1}{1 - \cos \theta} - \frac{1}{1 + \sin \theta}$

(d) $\frac{1}{1 + \cos \theta} - \frac{1}{1 - \sin \theta}$

102. If a line $y = 3x + 1$ cuts the parabola $x^2 - 4x - 4y + 20 = 0$ at A and B, then the tangents of the angle subtended by line segment AB at origin is

(a) $\frac{8\sqrt{3}}{205}$

(b) $\frac{8\sqrt{3}}{209}$

(c) $\frac{8\sqrt{3}}{215}$

(d) None of these

103. If a , b and c be three distinct real numbers in G.P. and $a + b + c = Xb$, then X cannot be

(a) 4

(b) -3

(c) -2

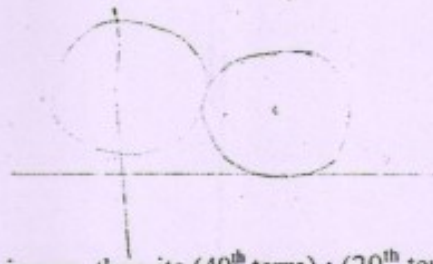
(d) 2

104. The number of three-digit numbers of the form xyz such that $x < y$ and $z \leq y$ is

- (a) 276
- (b) 266
- (c) 246
- (d) 244

105. A circle touches the x -axis and also touches the circle with centre $(0, 3)$ and radius 2. The locus of the centre of the circle is

- (a) a circle
- (b) an ellipse
- (c) a parabola
- (d) a hyperbola



106. If 19th term of a nonzero A.P. is zero, then its (49th term) : (29th term) is

- (a) 3:1
- (b) 4:1
- (c) 2:1
- (d) 1:3

107. The locus of centre of the circle touching the line $2x - y = 1$ at $(1, 1)$ is

- (a) $x + 3y = 2$
- (b) $x + 2y = 0$
- (c) $x + y = 2$
- (d) $2x - y = 1$

108. The positive value of λ for which the coefficient of x^2 in the expression

$$x^2 \left(\sqrt{x + \frac{\lambda}{x-1}} \right)^{10}$$

- (a) $\sqrt{5}$
(b) 4
(c) $2\sqrt{2}$
(d) 3
109. ABCD is a square of unit area. A circle is tangent to two sides of ABCD and passes through exactly one of its vertices. The radius of the circle is
- (a) $2 - \sqrt{2}$
(b) $\sqrt{2} - 1$
(c) $\frac{1}{2}$
(d) $\frac{1}{\sqrt{2}}$
110. If $a, b, c \in \mathbb{R}^+$, such that $a + b + c = 18$, then the maximum value of $a^{2a} b^{3b} c^4$ is equal to
- (a) $2^{18} \times 3^2$
(b) $2^{18} \times 3^3$
(c) $2^{18} \times 3^2$
(d) $2^{18} \times 3^3$
111. The equation of the plane bisecting the acute angle between the planes $2x - y + 2z + 3 = 0$ and $3x - 2y + 6z + 8 = 0$ is
- (a) $23x - 13y + 32z + 45 = 0$
(b) $5x - y - 4z = 3$
(c) $5x - y - 4z + 45 = 0$
(d) $23x - 13y + 32z + 3 = 0$

112. If the line $2x + y = 1$ is a normal to the parabola $y^2 = 4ax$, the possible value of x is

- (a) $2\sqrt{2}$
- (b) $\frac{1}{8}$
- (c) $4\sqrt{2}$
- (d) $\frac{1}{4}$

113. If the straight line $2x + y = 1$ is a normal to the parabola $y^2 = 4ax$, the triangle with origin as orthocentre, then the length of the hypotenuse is

- (a) (6, 4)
- (b) (-3, 3)
- (c) (-8, 8)
- (d) (0, 7)

Handwritten work for Q113:

$$2x + y = 1 \Rightarrow x = -\frac{y}{2} + \frac{1}{2}$$

$$2(-\frac{y}{2}) + 2y - 1 = 0$$

$$-y + 2y - 1 = 0 \Rightarrow y = 1$$

114. For $x^2 - (a+3)x + 4 = 0$ to have real solutions, the range of a is

- (a) $(-\infty, -7] \cup [1, \infty)$
- (b) $(-3, \infty)$
- (c) $(-\infty, -7]$
- (d) $[1, \infty)$

Handwritten work for Q114:

$$x^2 - (a+3)x + 4 = 0$$

$$D \geq 0$$

$$(a+3)^2 - 16 \geq 0$$

$$a^2 + 6a + 9 - 16 \geq 0$$

$$a^2 + 6a - 7 \geq 0$$

$$(a+7)(a-1) \geq 0$$

$$a \leq -7 \text{ or } a \geq 1$$

115. The line $2x + y = 1$ touches a hyperbola and passes through the point of intersection of a directrix and the x -axis. The equation of hyperbola is

- (a) $\frac{x^2}{1} - \frac{y^2}{3} = 1$
- (b) $\frac{x^2}{1} - \frac{y^2}{3} = 2$
- (c) $\frac{x^2}{3} - \frac{y^2}{1} = 1$
- (d) $\frac{x^2}{3} - \frac{y^2}{1} = 2$

116. Let $A = \{x_1, x_2, x_3, \dots, x_7\}$, $B = \{y_1, y_2, y_3\}$. The total number of functions $f: A \rightarrow B$ that are onto and there are exactly three elements x in A such that $f(x) = y_1$ is
- (a) 490
 (b) 510
 (c) 630
 (d) None of these
117. If the intercepts made on the line $y = mx$ by the lines $y = 2$ and $y = 6$ are less than 5, then the range of values of m is
- (a) $(-\infty, -3) \cup (2/3, \infty)$
 (b) $(-4/3, 4/3)$
 (c) $(-3/4, 4/3)$
 (d) none of these
118. If the maximum value of $y = a \cos x - \frac{1}{3} \cos 3x$ occurs when $x = \frac{\pi}{6}$, then the value of a is
- (a) -2
 (b) 2
 (c) $\frac{2}{\sqrt{3}}$
 (d) $-\frac{2}{\sqrt{3}}$

116. Let $A = \{x_1, x_2, x_3, \dots, x_7\}$, $B = \{y_1, y_2, y_3\}$. The total number of functions $f: A \rightarrow B$ that are onto and there are exactly three elements x in A such that

- (a) 300
- (b) 510
- (c) 630
- (d) None of these

117. If the intercepts made on the line $y = mx$ by lines $y = 2$ and $y = 6$ is less than 5, then the range of values of m is

- (a) $(-4, -1) \cup (1, 2)$
- (b) $(-4/3, -1/3)$
- (c) $(-3/4, 4/3)$
- (d) none of these

118. If the maximum value of $y = a \cos x - \frac{1}{3} \cos 3x$ occurs when $x = \frac{\pi}{6}$, then the value of a is

- (a) -2
- (b) 2
- (c) $\frac{2}{\sqrt{3}}$
- (d) $-\frac{2}{\sqrt{3}}$

119. The number of points in the rectangle $\{(x, y) : -12 \leq x \leq 12 \text{ and } -3 \leq y \leq 3\}$ which lie on the curve $y = x + \sin x$ and at which the tangent to the curve is parallel to the x-axis is

- (a) 0
- (b) 2
- (c) 4
- (d) 8

120. The last digit of $(1! + 2! + 3! + \dots + 2005!)^{2005}$ is

- (a) 9
- (b) 2
- (c) 7
- (d) 1

121. The area bounded by the circle $x^2 + y^2 = 8$, the parabola $x^2 = 2y$ and the line $y = x$ in $y \geq 0$ is

- (a) $\frac{2}{3} + 2\pi$
- (b) $\frac{2}{3} - 2\pi$
- (c) $\frac{2}{3} + \pi$
- (d) $\frac{2}{3} - \pi$

122. The constraints

$$\begin{aligned} -x_1 + x_2 &\leq 1 \\ -x_1 + 3x_2 &\leq 9 \\ x_1, x_2 &\geq 0 \end{aligned}$$

defines on

- (a) Bounded feasible space
- (b) Unbounded feasible space
- (c) Both bounded and unbounded feasible space
- (d) None of these

123. If α is a real number, then the value of $\int \frac{dx}{\cos(x + \alpha) + \sin \alpha}$ is

(b) $\sqrt{2}(\tan x + \tan \alpha) + C$; where C is an arbitrary constant

(c) $\sqrt{\frac{2(\tan x + \tan \alpha)}{\sin \alpha}} + C$; where C is an arbitrary constant

(d) $\sqrt{\frac{2(\tan x + \tan \alpha)}{\cos \alpha}} + C$; where C is an arbitrary constant

124. The value of $\int \frac{dx}{x + \sqrt{x^2 - 1}}$ is

(a) $\log(\sqrt{2} + 1)$

(b) $\frac{1}{\sqrt{2}} \log(\sqrt{2} + 1)$

(c) $\sqrt{2} \log(\sqrt{2} - 1)$

(d) $\frac{1}{\sqrt{2}} \log(\sqrt{2} - 1)$

125. A bag contains 30 white balls and 10 red balls. 16 balls are drawn one-by-one randomly from the bag with replacement. If X be the number of white balls drawn, then $\left(\frac{\text{mean } X}{\text{standard deviation of } X} \right)$ is equal to

(a) 4

(b) $\frac{4\sqrt{3}}{3}$

(c) $4\sqrt{3}$

(d) $3\sqrt{2}$

white = 30
red = 10

126. The value of $\int_0^{\pi} x \sin x$ is

(b) $\pi\left(\frac{\pi}{2} + 1\right)$

(c) $\pi\left(\frac{\pi}{3} - 1\right)$

(d) $\pi\left(\frac{\pi}{3} + 1\right)$

127. If the probability of hitting a target in a single shot is $\frac{1}{6}$, then the minimum number of independent shots at the target required by him so that the probability of hitting the target at least once is greater than $\frac{5}{6}$, is

(a) 6

(b) 5

(c) 4

(d) 3

128. The solution of the differential equation $\frac{dy}{dx} + y \cos x = \frac{\sin 2x}{2}$, is

(a) $ye^{\sin x} = C + e^{2\sin x}(\sin x - 1)$

(b) $ye^{\sin x} = C + e^{\sin x}(\sin x - 1)$

(c) $ye^{\sin x} = C + e^{-\sin x}(\sin x + 1)$

(d) $ye^{\sin x} = C + e^{-2\sin x}(\sin x - 1)$; C being an arbitrary constant

129. A data consists of n observations x_1, x_2, \dots, x_n . If $\sum_{i=1}^n (x_i + 1)^2 = 9n$ and

- (a) 5
- (b) $\sqrt{5}$
- (c) $\sqrt{7}$
- (d) 2

130. The order and the degree of the differential equation of radius r is

- (a) 2, 3
- (c) 2, 2
- (d) 3, 3

131. Let $d \in \mathbb{R}$, and

$$A = \begin{bmatrix} -2 & 4+d & \sin \theta - 2 \\ 1 & \sin \theta + 2 & d \\ 5 & 2\sin \theta - d & -\sin \theta + 2 + 2d \end{bmatrix}$$

$\theta \in [0, 2\pi]$. If minimum value of $\det(A) = \xi$, then a value of d is

- (a) -7
- (b) $2(\sqrt{2} + 2)$
- (c) -5
- (d) $2(\sqrt{2} + 1)$

132. The values of a, b and c which make $f(x)$

$$f(x) = \begin{cases} \frac{\sqrt{x+bx^2}-\sqrt{ax}}{bx^{3/2}} & x > 0 \\ \end{cases}$$

continuous at $x = 0$ are

(a) $a = \frac{-3}{2}, b = 0, c = \frac{1}{2}$

(c) $a = \frac{-1}{2}, b = 0, c = \frac{1}{2}$

(d) None of these

133. Let $A = \begin{bmatrix} 2 & b & 1 \\ b & b^2+1 & b \\ 1 & b & 2 \end{bmatrix}$ where $b > 0$. Then the minimum value of $\frac{\det(A)}{b}$ is

(a) $\sqrt{3}$

(b) $-\sqrt{3}$

(c) $-2\sqrt{3}$

(d) $2\sqrt{3}$

134. The function

$$f(x) = x - |x - x^2|, -1 \leq x \leq 1$$

is continuous on the interval

(a) $[-1, 1]$

(b) $(-1, 1)$

(c) $[-1, 1] \setminus \{0\}$

(d) $(-1, 1) \setminus \{0\}$

(a) $\frac{22}{23}$

(b) $\frac{23}{22}$

(c) $\frac{21}{22}$

136. A plane which is passing through the point (5, 2, 6) and the line

$$\frac{x-3}{1} = \frac{y-6}{5} = \frac{z-4}{4} \text{ is}$$

(a) $x - y + z = 1$

(b) $x + y + z = 1$

(c) $x - y + 2z = 0$

(d) $x + y + 2z = 0$

137. Let $f(x+y) = f(x)f(y)$ for all x, y , where $f(0) \neq 0$. If $f(0) = 2$, then $f(x)$ is equal to

(a) Ae^x

(b) Ae^{2x}

(c) $2x$

(d) $2Ax$

13. If the vector

- (a) 1
- (b) $\frac{1}{2}$
- (c) $\frac{1}{3}$
- (d) $\frac{1}{4}$

- (a) has no limit
- (b) is discontinuous
- (c) is continuous but not differentiable
- (d) is differentiable

140. The vector projection of a vector $i + k$ on y-axis is
- (a) 1
 - (b) 2
 - (c) 0
 - (d) $\sqrt{3}$

141. Locus of the point of intersection of the tangent at the end points of the focal chord of the ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$, ($b < a$) is a/an
- (a) circle
 - (b) ellipse
 - (c) hyperbola
 - (d) pair of straight line

UEBT/D

(a) 0

(b) $\frac{1}{8}$

143. A perpendicular is drawn from a point $(1, 2, 3)$ to the line $\frac{x-1}{2} = \frac{y-2}{3} = \frac{z-3}{4}$

The coordinates of the foot of perpendicular is

(a) (1, 3, 5)

(b) (0, 3, -2)

(c) (2, 4, 7)

(d) (1, 3, 4)



144. Which of the following statements is always true?

(a) If $f(x)$ is increasing, then $f^{-1}(x)$ is decreasing

(b) If $f(x)$ is decreasing, then $\frac{1}{f(x)}$ is also increasing

(c) If f and g are positive function and f is increasing and g is decreasing, then $\frac{f}{g}$ is a decreasing function

(d) If f and g are positive function and f is decreasing and g is increasing, then $\frac{f}{g}$ is a decreasing function

(b) 1

(c) 3

(d) 4

(a) $(-\infty, 2) \cup (3, \infty)$

(c) $(-\infty, 0)$

(d) $[2, 3]$

147. If z is a complex number of unit modulus and argument θ , then $\arg\left(\frac{1-z}{1+z}\right)$

equals to

(a) $-\theta$

(b) $\frac{\pi}{2} - \theta$

(c) θ

(d) $4 - \theta$

148. Let $f(x) = ax^3 + bx^2 + cx - 1$ have extrema at $x = \alpha, \beta$ such that $\alpha\beta < 0$ and $f(\alpha)f(\beta) < 0$. Then the equation $f(x) = 0$ has

(a) three equal roots

(b) one negative root if $f(\alpha) < 0$ and $f(\beta) > 0$

(c) one positive root if $f(\alpha) > 0$ and $f(\beta) < 0$

(d) None of these